

# The measurement

$$C = \frac{\Delta Q}{\Delta T}$$



# How to measure $C_p$ ?

• Principle : apply  $P$ , read  $T$  and time

• adiabatic : isolated sample and pt by pt  $C = \frac{\Delta Q}{\Delta T}$   
quasi-adiabatic, continuous heating  $P = C dT/dt$

• relaxation : heat pulse, thermal link to  $T$  bath  
large relaxation, dual slope, ...

• modulation : alternative heating at  $\omega$   $T_{ac} = \frac{P}{K + jC\omega}$



# very demanding T measurements !!

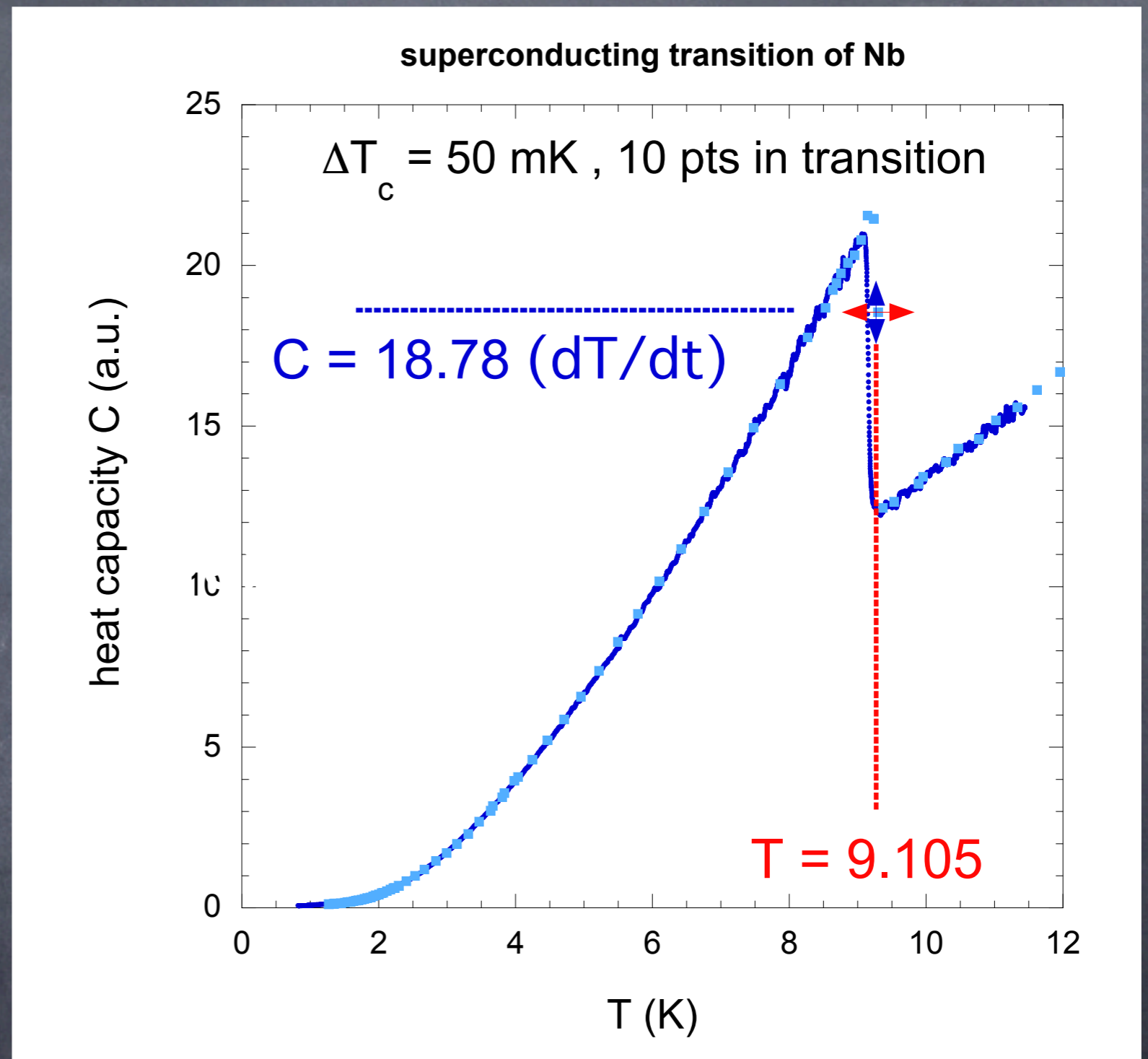
$$DC/C \sim 10^{-3}$$

$$T = 9.104785$$

$$dT/T \sim 10^{-3}$$

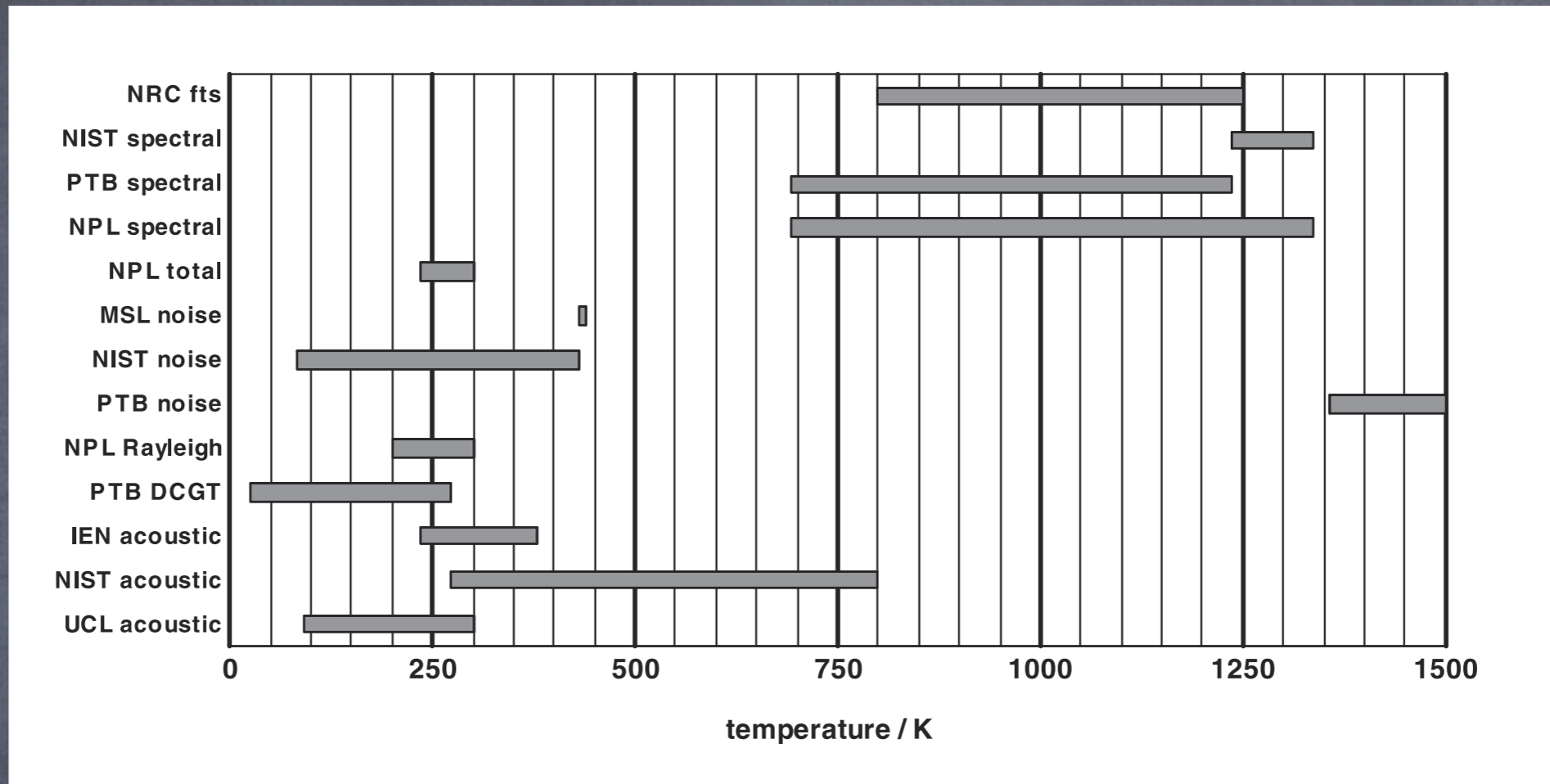
and TIME

calibrations of  
thermometers is a  
nightmare !!  
and fitting procedure

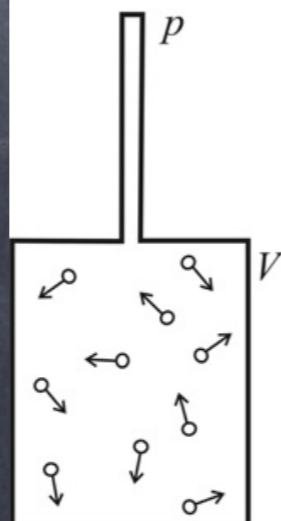




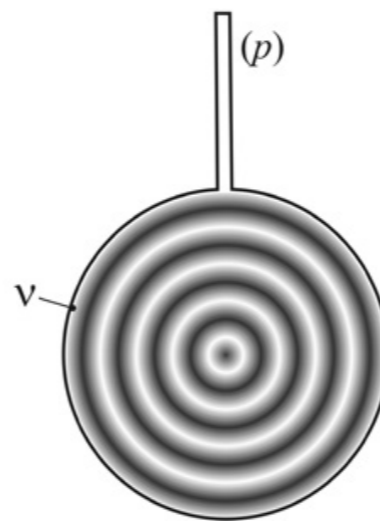
# Thermodynamic thermometers



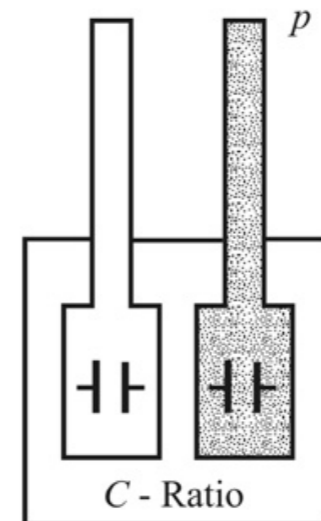
CVGT  
 $p V = n R T$



AGT  
 $c = (\gamma R T / M)^{1/2}$



DCGT  
 $p = k T (\epsilon - \epsilon_0) / \alpha_0$



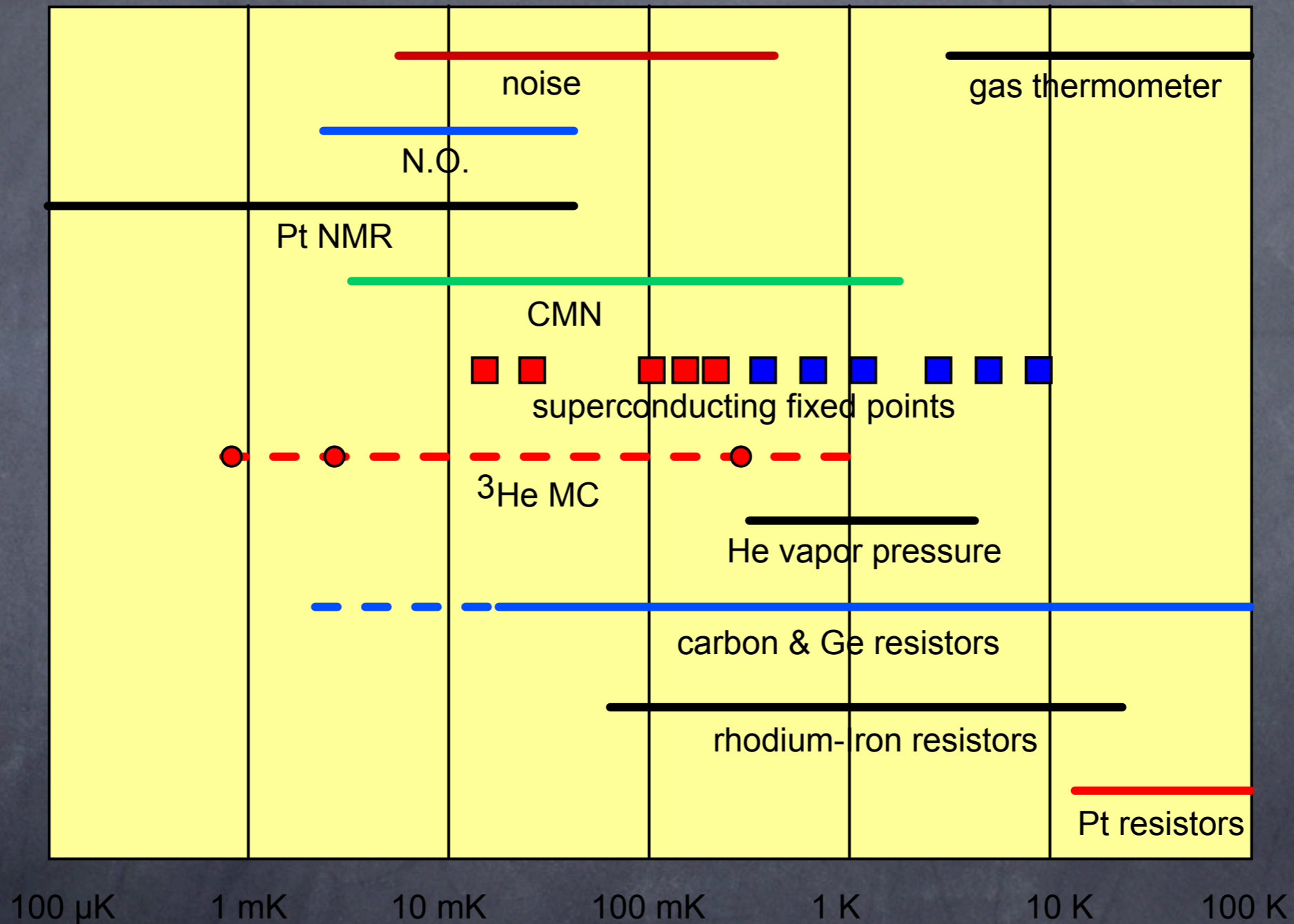


# Thermometers

- What is a good thermometer ?
- primary / secondary
- accuracy
- resolution/sensitivity
- reproducibility
- easy to use
- time response



# Thermometers actually used in low temperature laboratory





# ADIABATIC

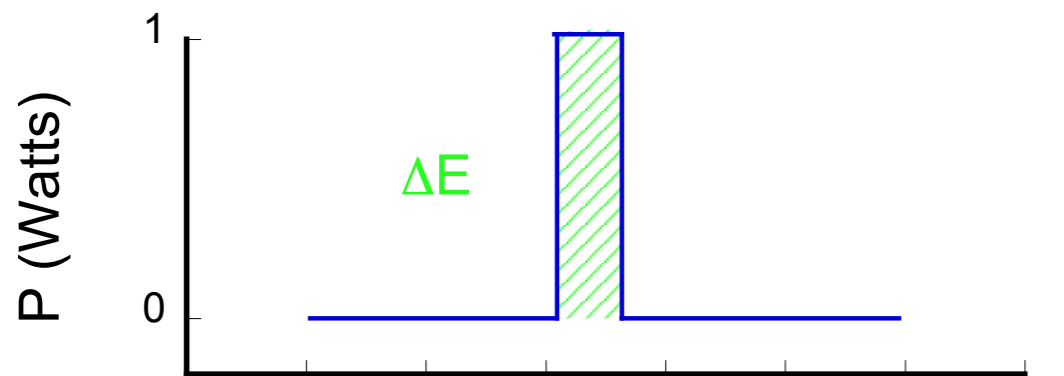
heat pulse and isolated sample

- Excellent precision and accuracy

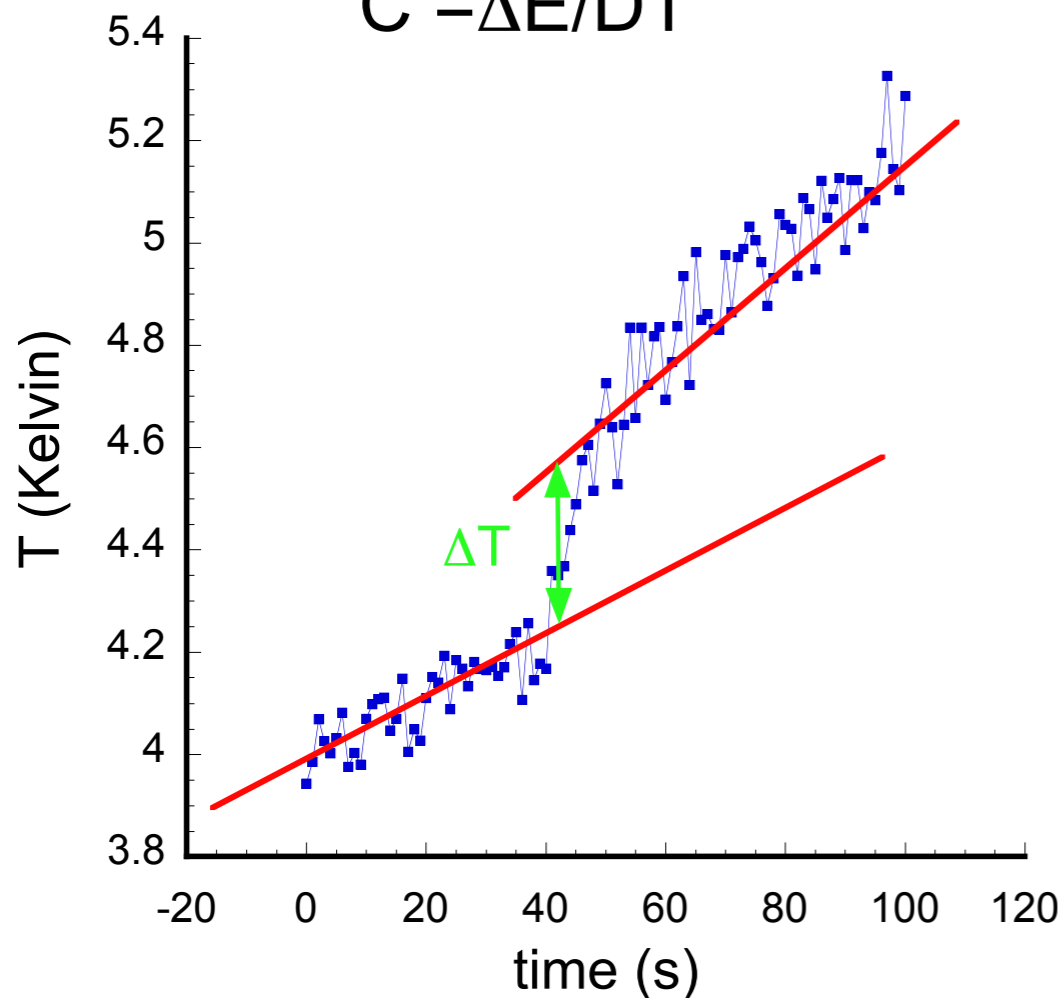
$\lambda$  transition in space shuttle

but

- method point by point (tenuous)
- how to cool the sample ?
- limited to large samples (parasitic non-adiabaticity)



$$C = \Delta E / \Delta T$$

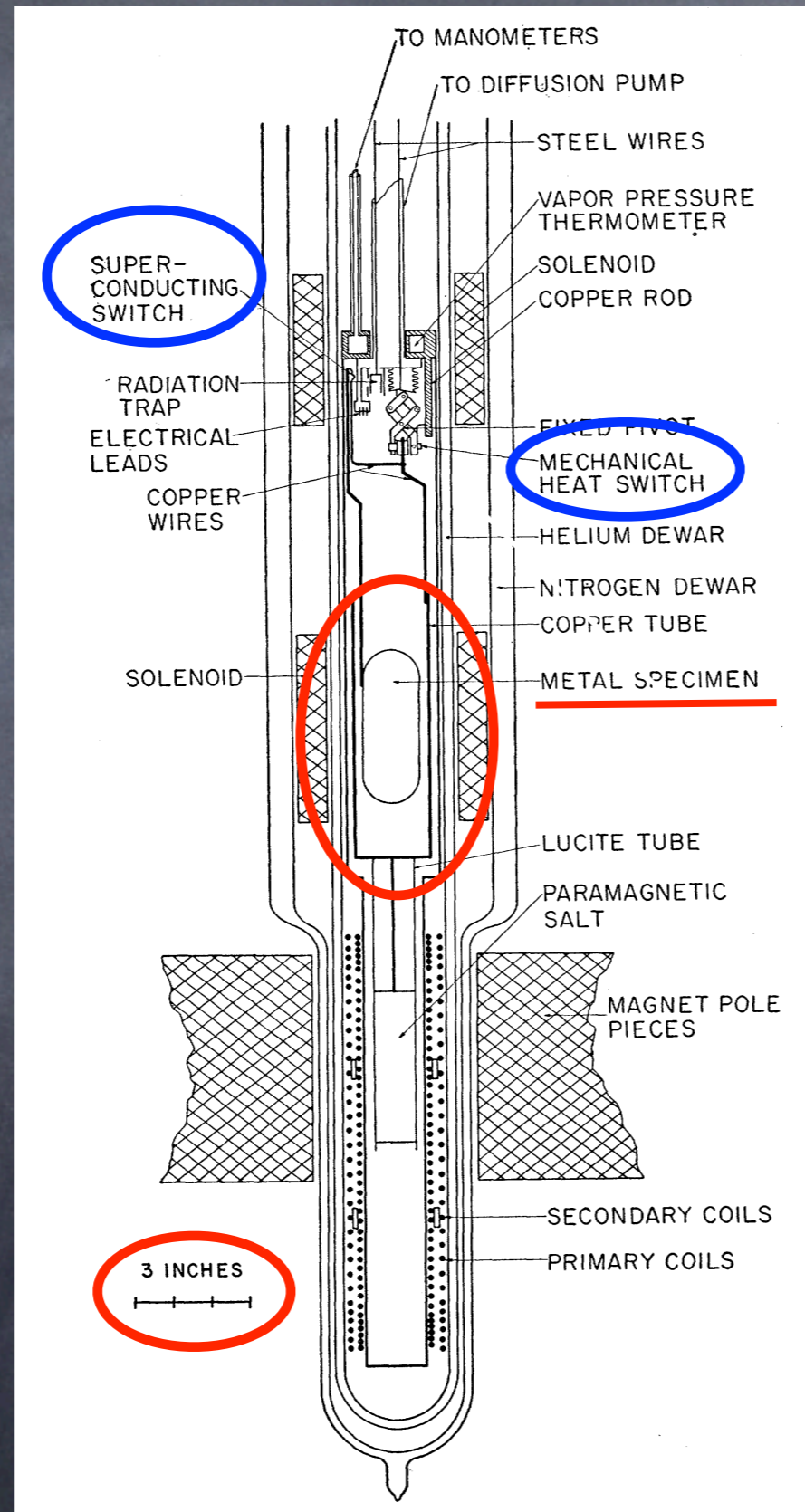




# Apparatus used for calorimetric measurements in the adiabatic demagnetization range

Prof. N.E. Phillips  
University of California  
BERKELEY

Superconducting  
switch



Mechanical heat  
switch

Sample



# Apparatus used for calorimetric measurements in the adiabatic demagnetization range

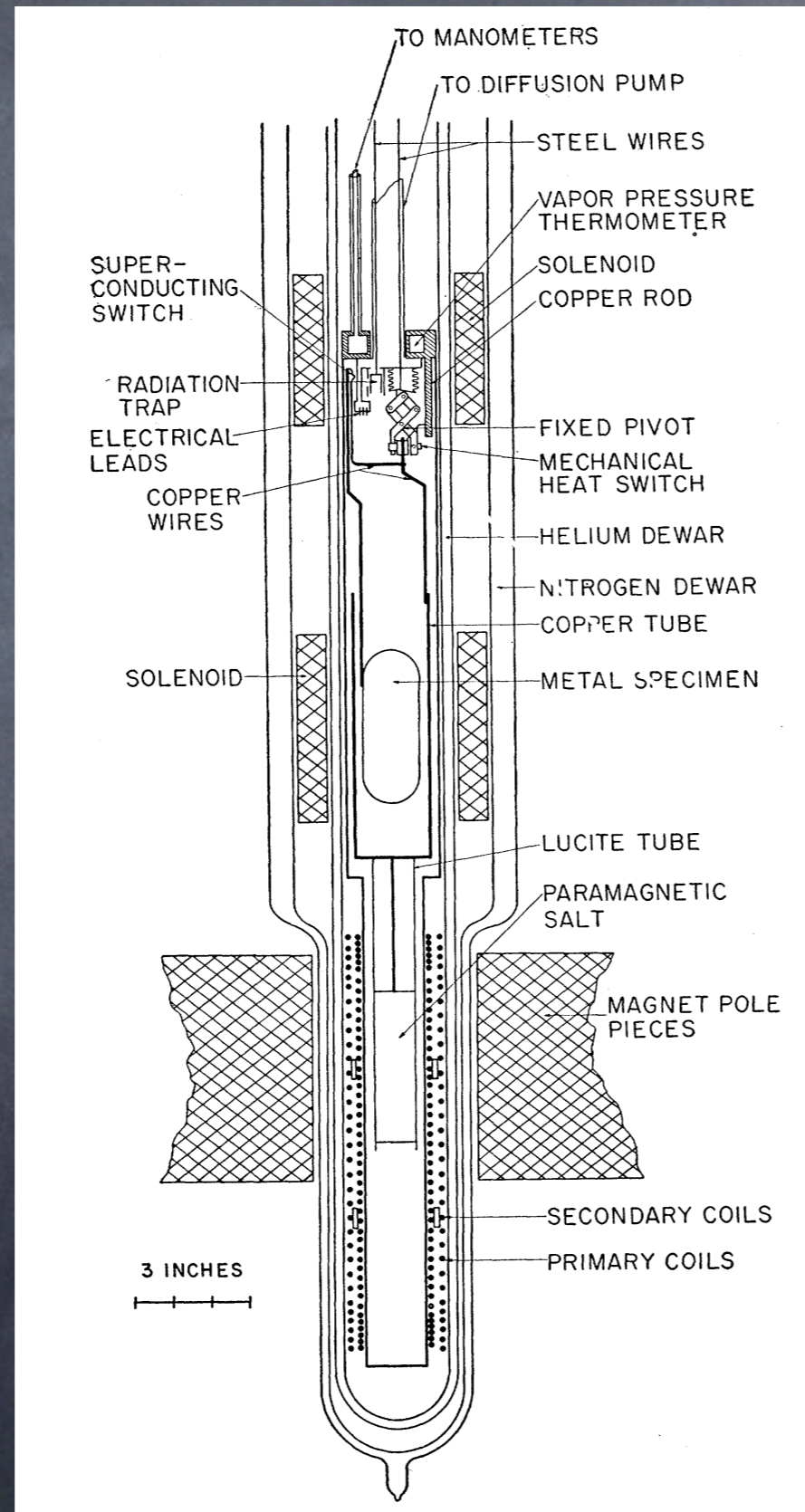
Prof. N.E. Phillips  
University of California  
BERKELEY

100mK-40K

accuracy a few %

$\Delta C/C$  a few  $10^{-3}$

100mg-1g Heavy Fermion

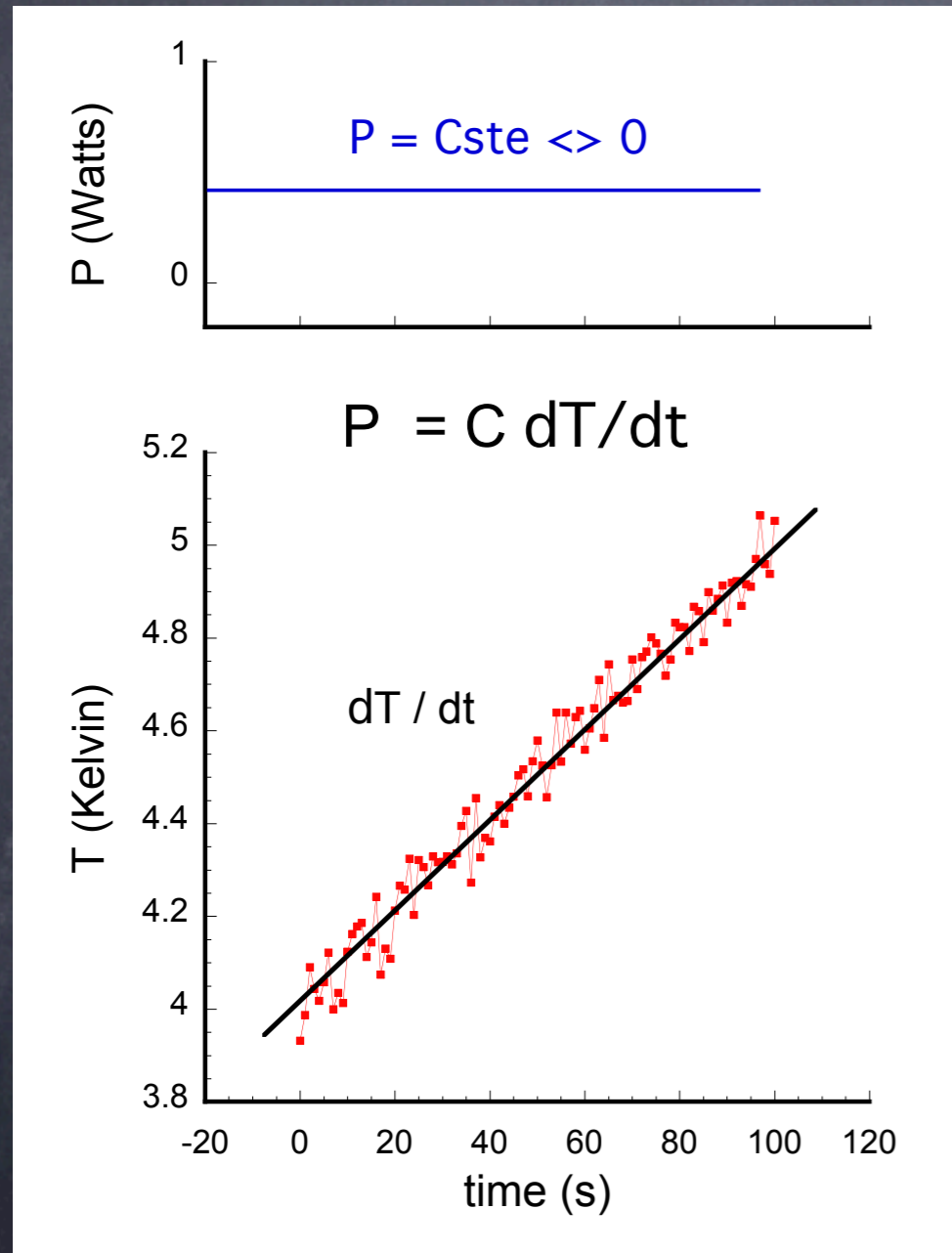




# QUASI-ADIABATIC

Prof. A. Junod  
University of Geneva

~~heat pulse~~ continuous heating  
and still isolated sample

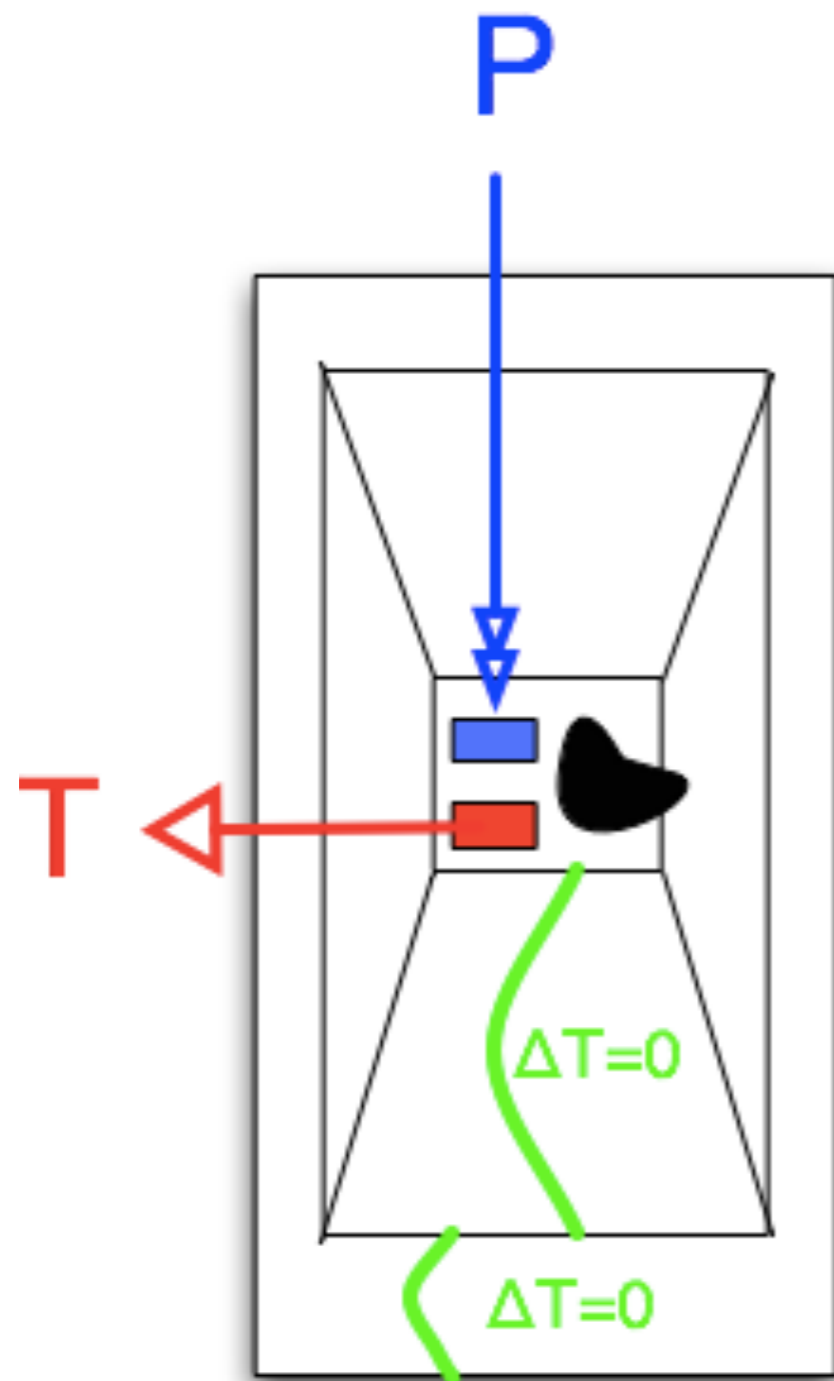




# QUASI-ADIABATIC

Prof. A. Junod  
University of Geneva

~~heat pulse~~ continuous heating  
and still isolated sample



Double radiation shields  
but still

$P_{\text{parasitic}}$  a few  $10^{-7}\text{W}$   
with

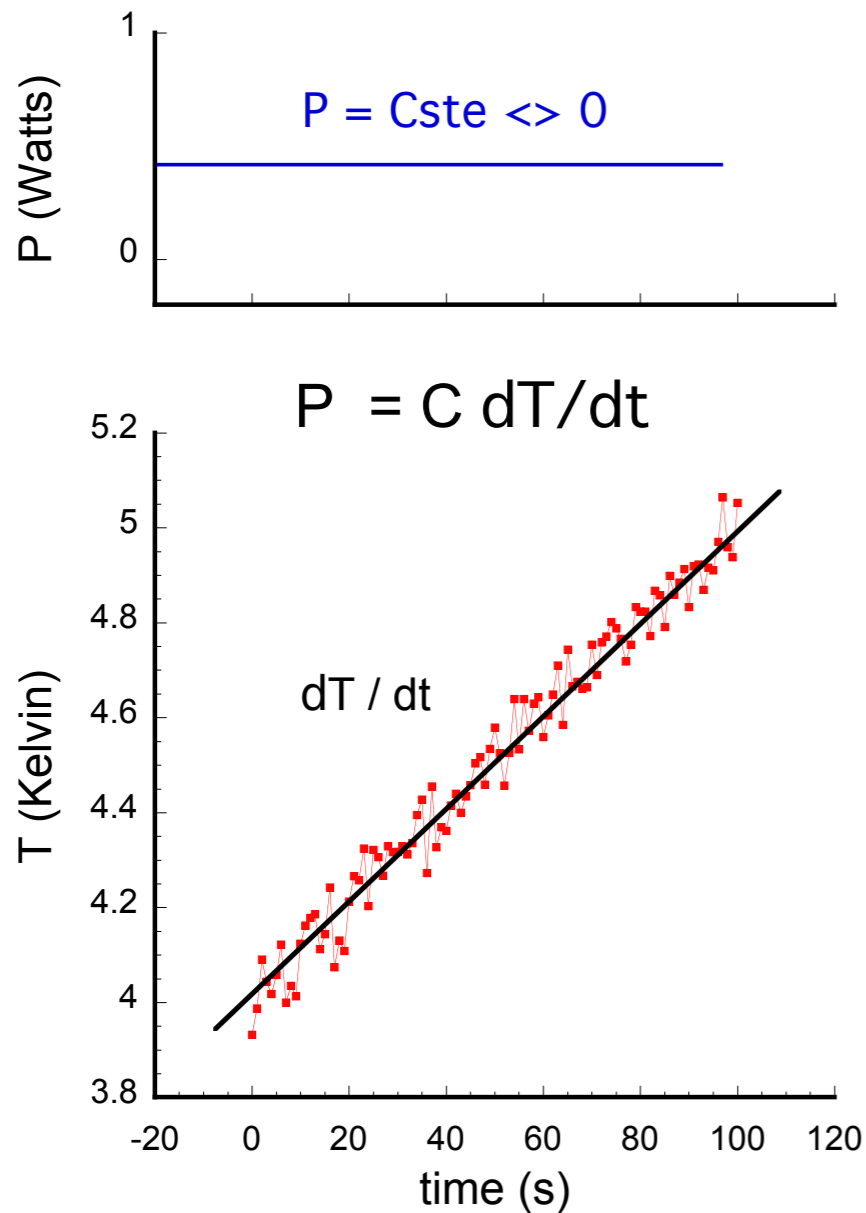
$\Delta T$  measured via  
Cr-Cn thermocouples  
and nanovoltmeter



# QUASI-ADIABATIC

Prof. A. Junod  
University of Geneva

~~heat pulse~~ continuous heating  
and still isolated sample



10K-300K

accuracy 1-5 %

$\Delta C/C$  a few  $10^{-3}$

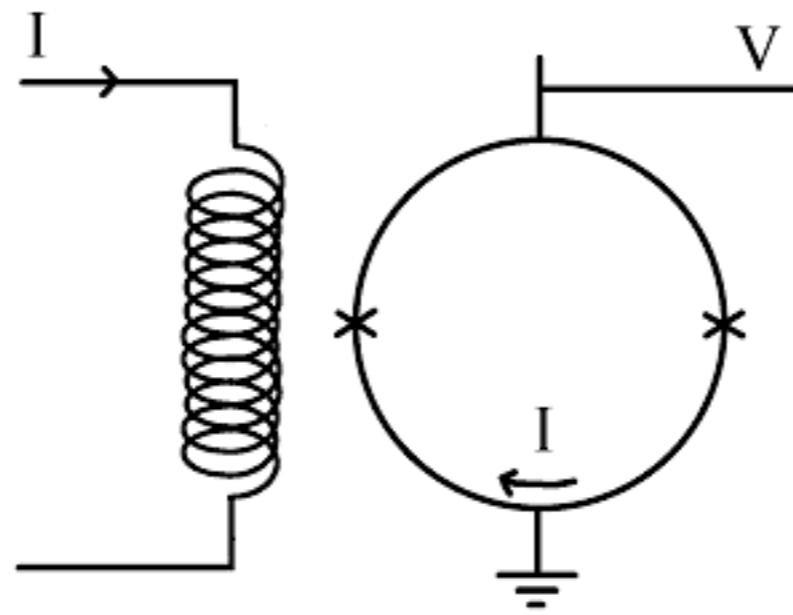
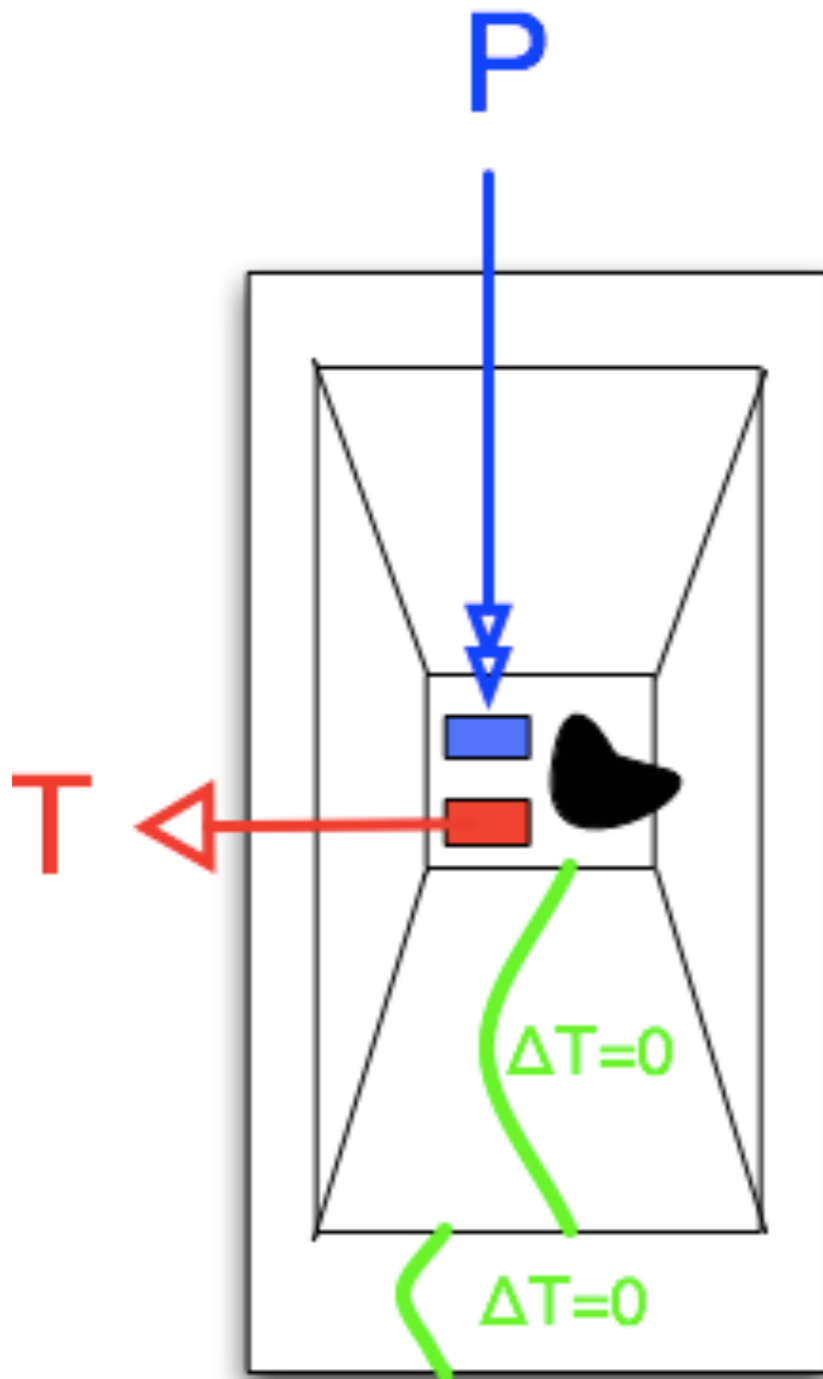
10mg-100g HTSC



# QUASI-ADIABATIC in dilution range

R. Calemczuk  
CEA-grenoble

$\Delta T$  measured via  
Au:Fe thermocouples  
and SQUID !!

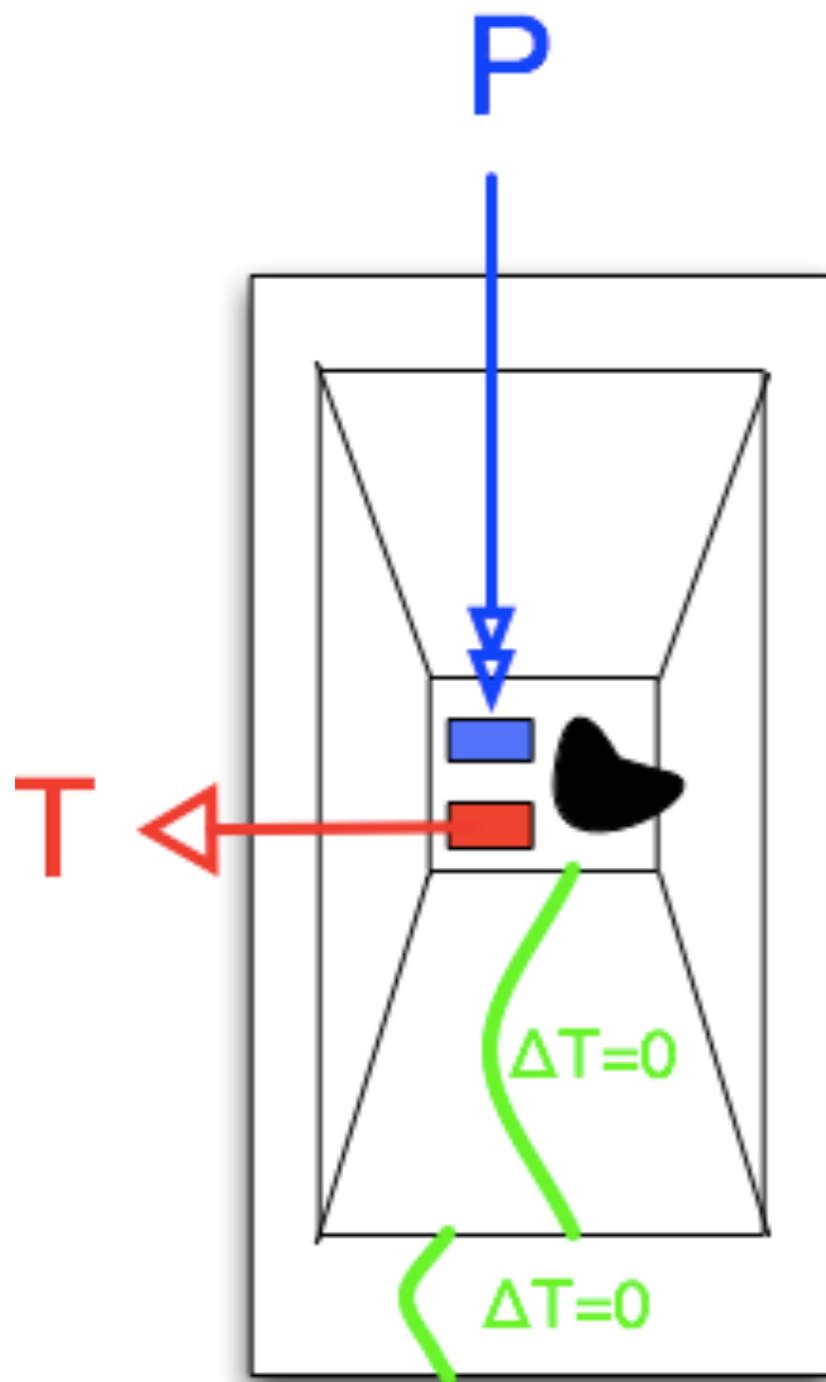


SQUID + Chopper =  $1-2 \text{ pA}/(\text{Hz})^{1/2}$



# QUASI-ADIABATIC in dilution range

R. Calemczuk  
CEA-grenoble



at 100 mK

$$\sqrt{V^2} = \sqrt{4k_B T R} = 0.5 \text{ pV}/\sqrt{\text{Hz}}$$

$$\sqrt{I^2} = \sqrt{4k_B T / R} = 10 \text{ pA}/\sqrt{\text{Hz}}$$

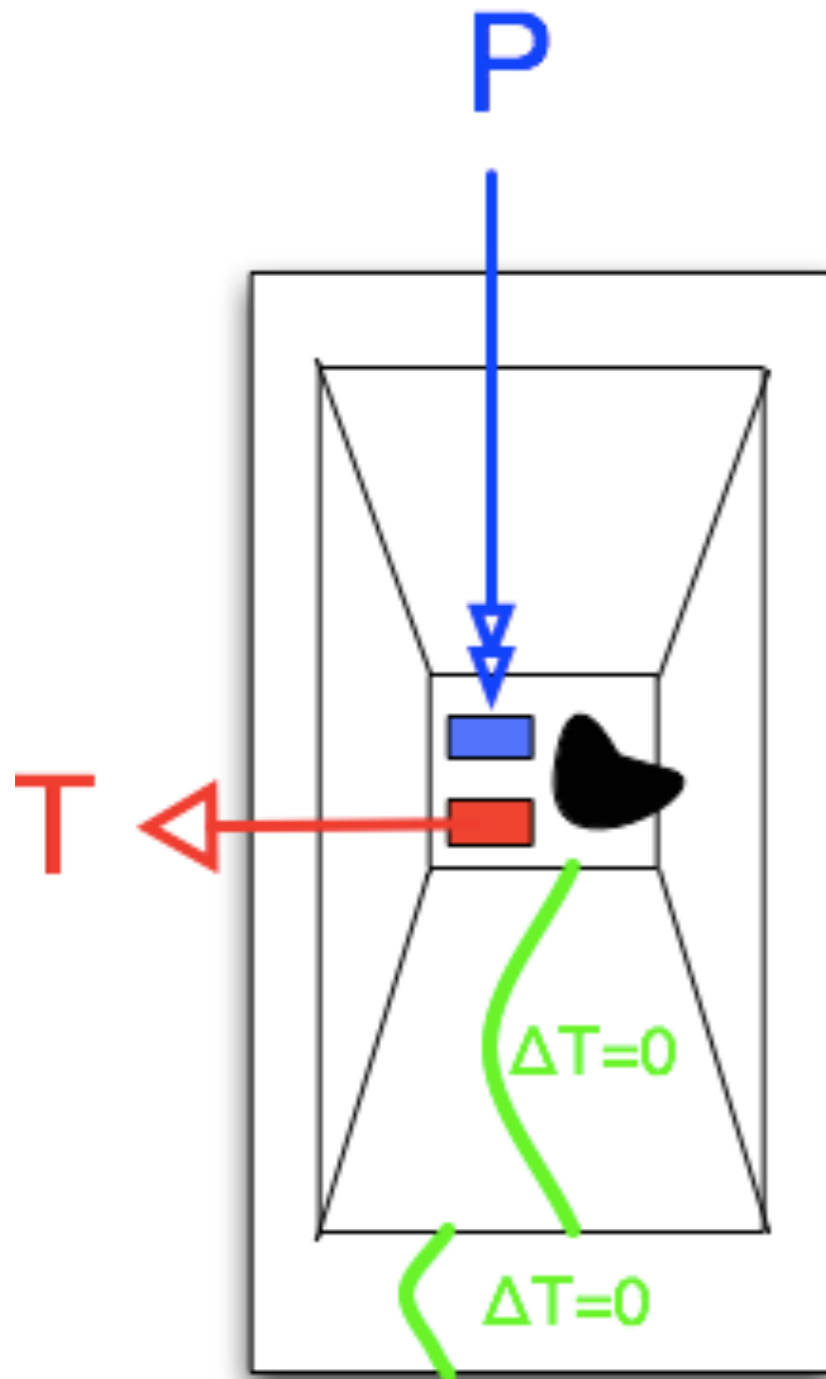
$$\sqrt{\Delta T^2} = 2 \text{ } \mu\text{K}/\sqrt{\text{Hz}}$$

$$P_{\text{parasitic}} = \frac{L}{S/T} \sqrt{I^2} = 10^{-13} \text{ W}$$



# QUASI-ADIABATIC in dilution range

R. Calemczuk  
CEA-grenoble

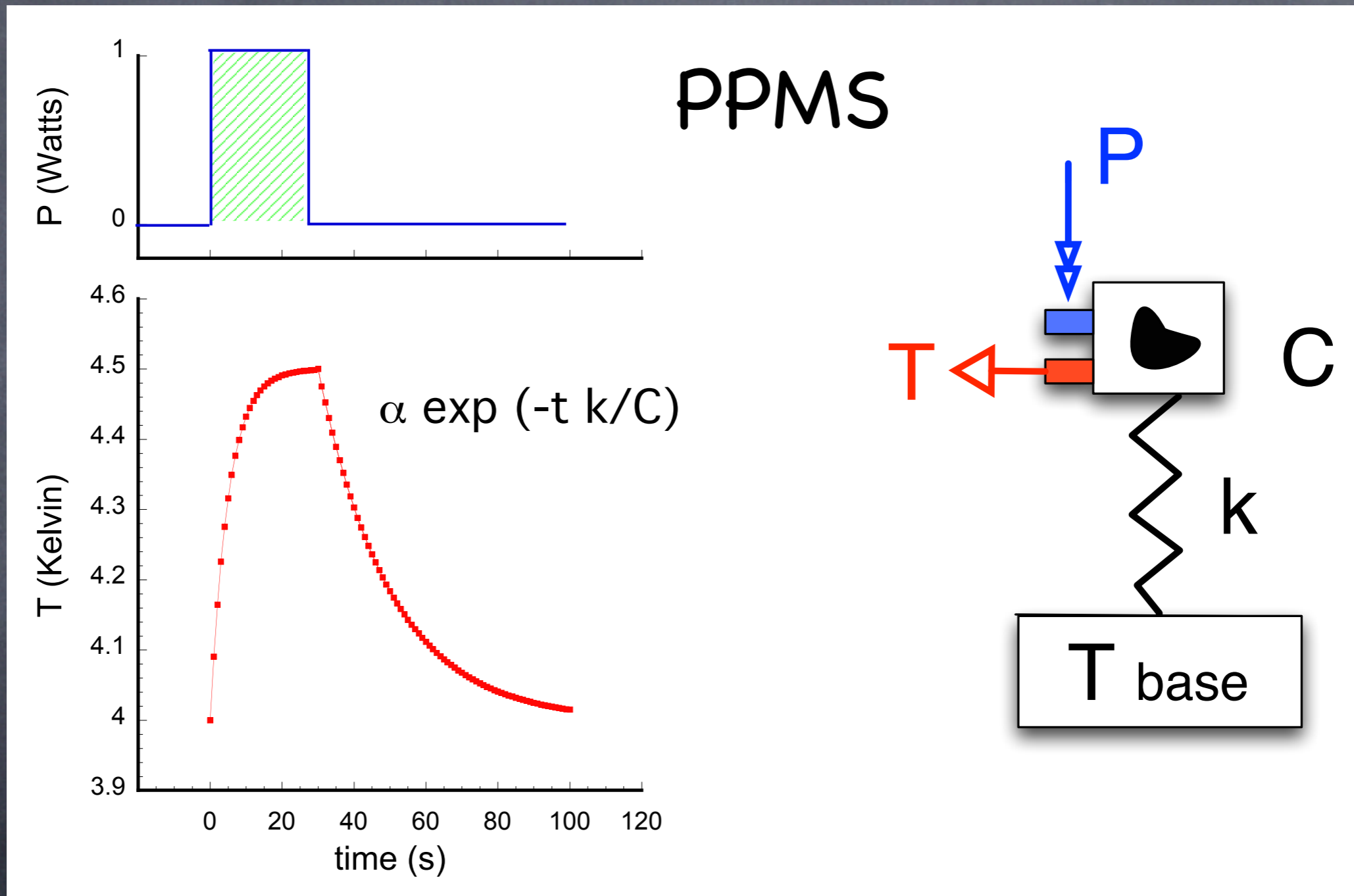


1-10% of 10mg Cu  
BUT !!  
no calibration of S  
(null detector)  
 $\Delta T = 0$   
therefore thermometer  
in compensated area



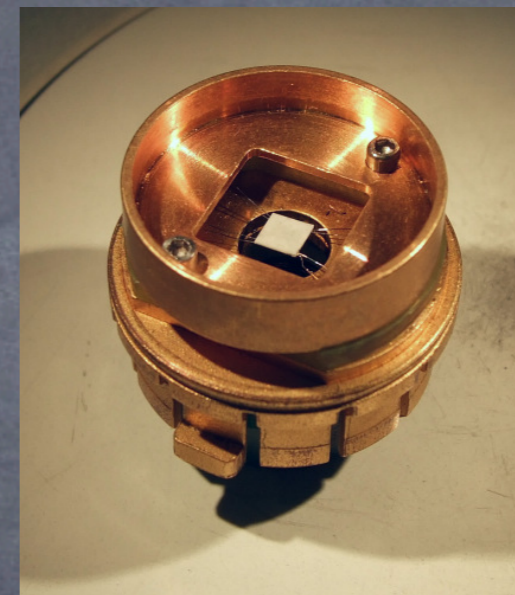
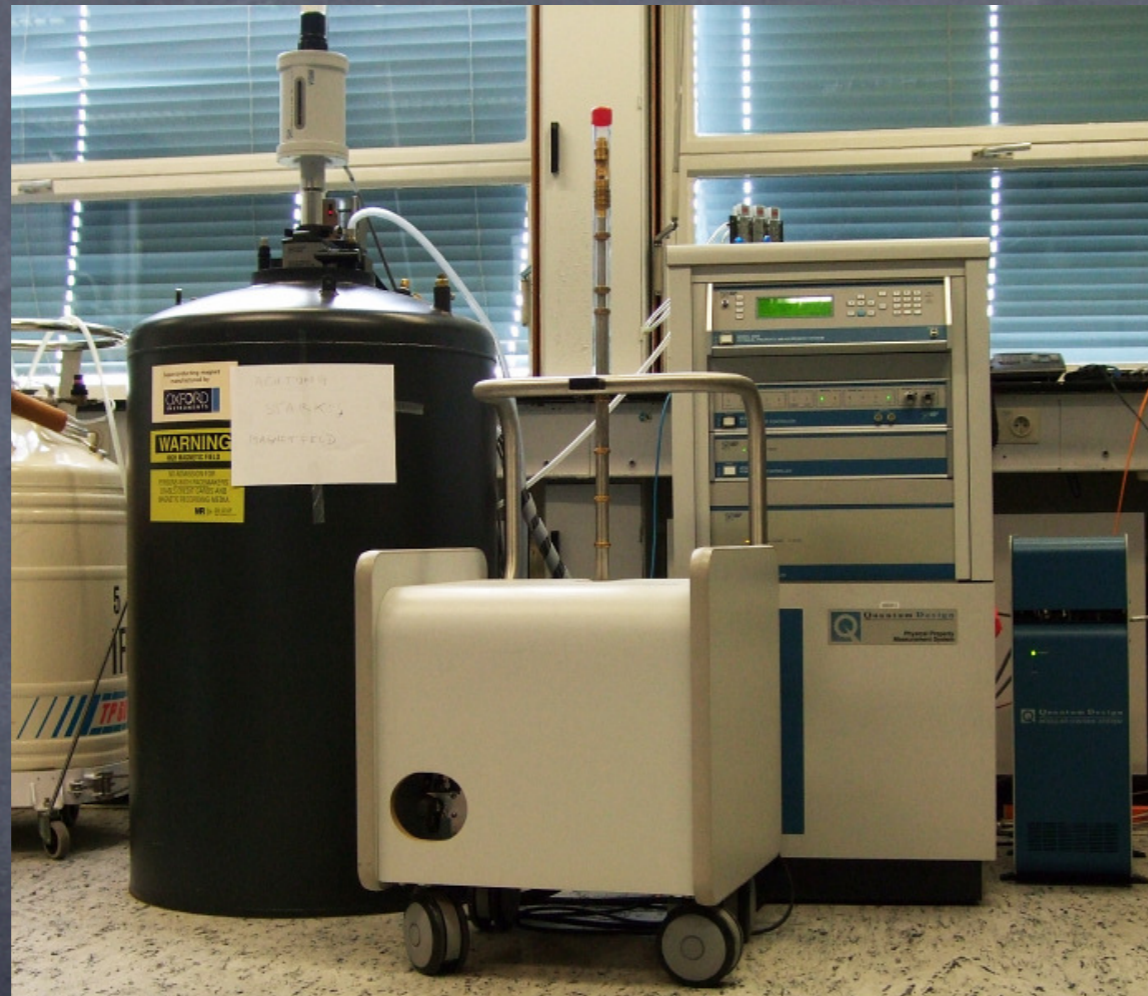
# RELAXATIONS Methods

heat pulse or steplike, heat link to thermal bath at  $T_b$





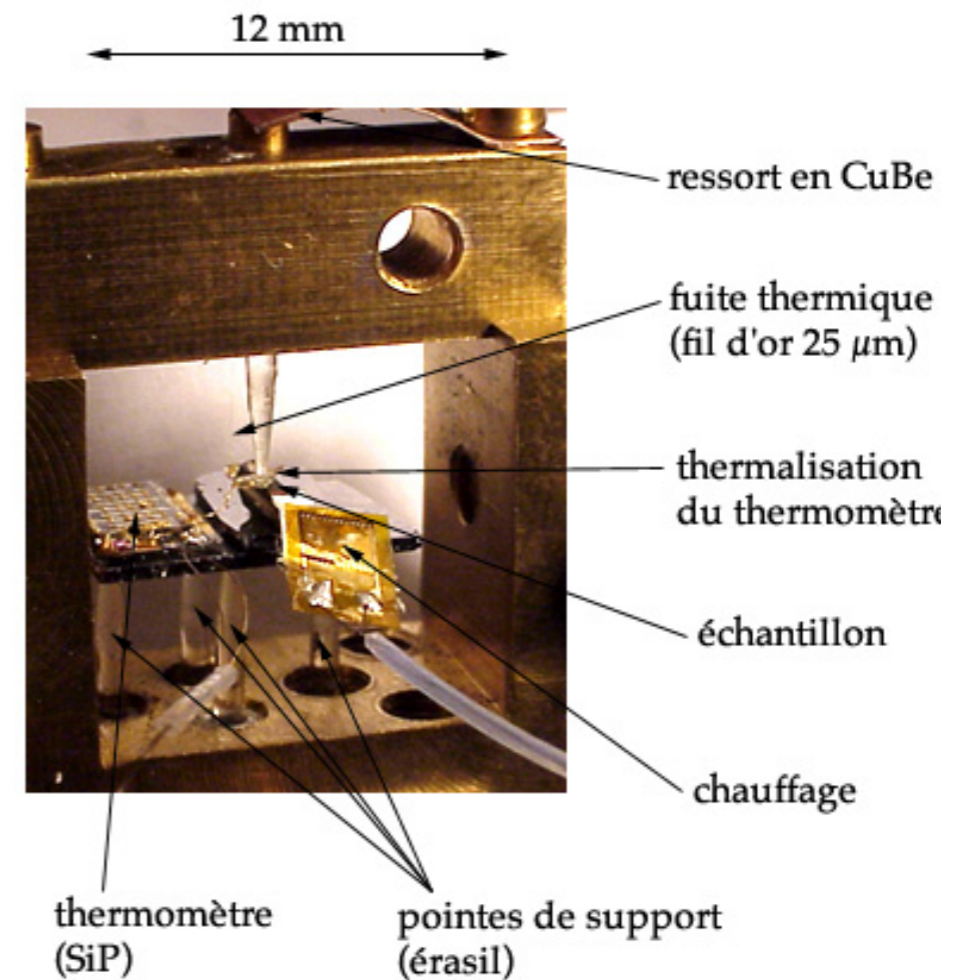
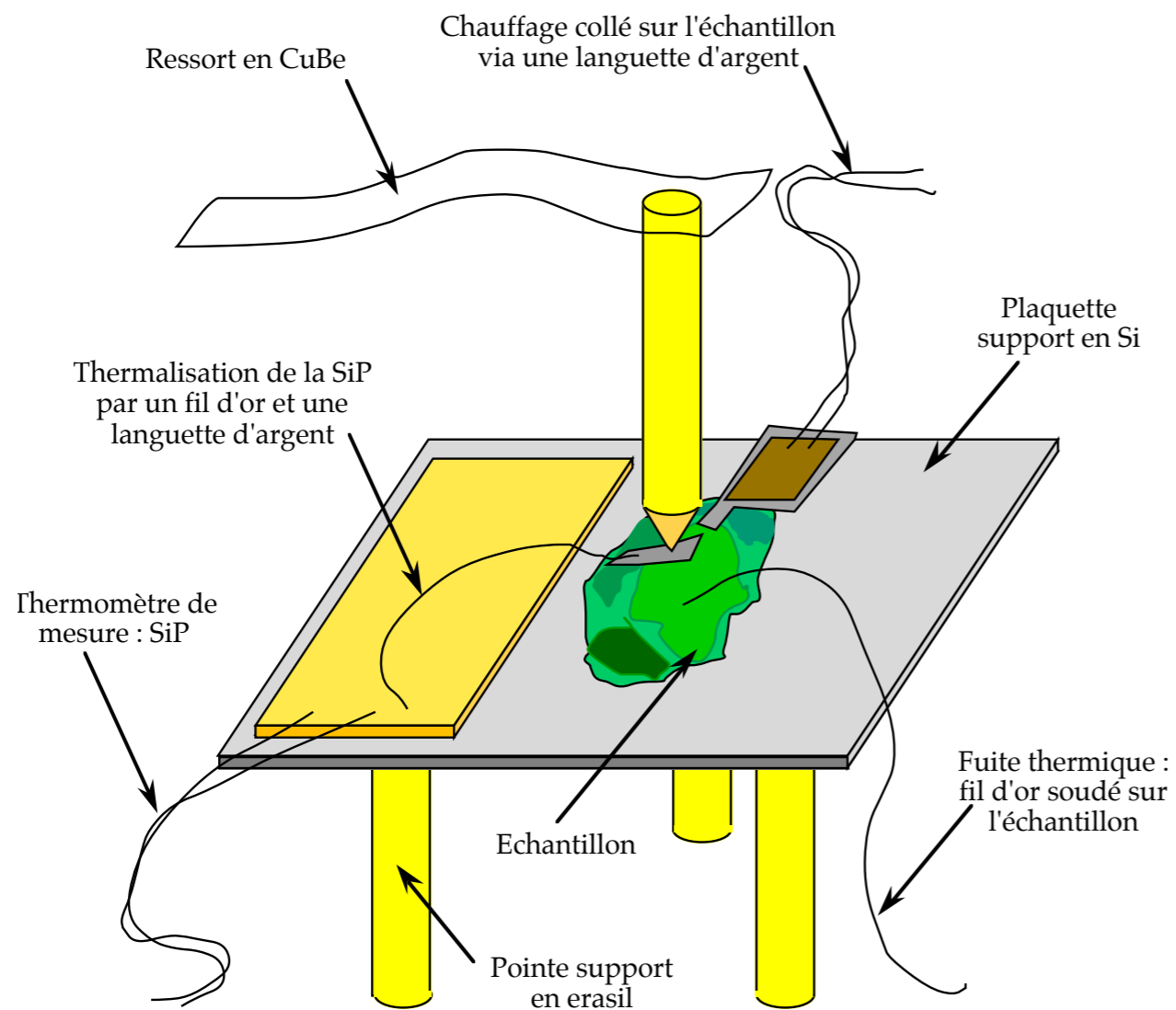
# PPMS Quantum Design : $^4\text{He}$ and $^3\text{He}$





# Set-up at ultra-low T (10mk-1K)

J.P. Brison  
CEA-grenoble





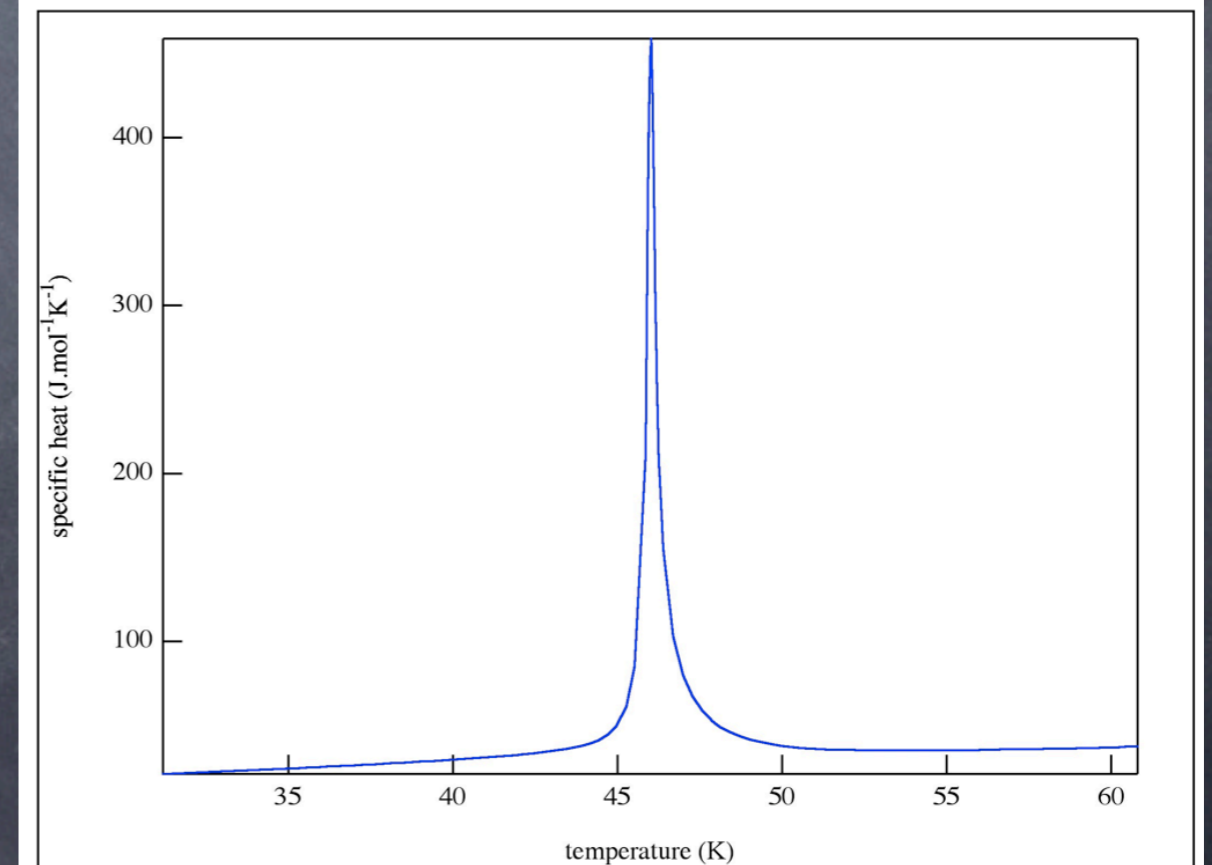
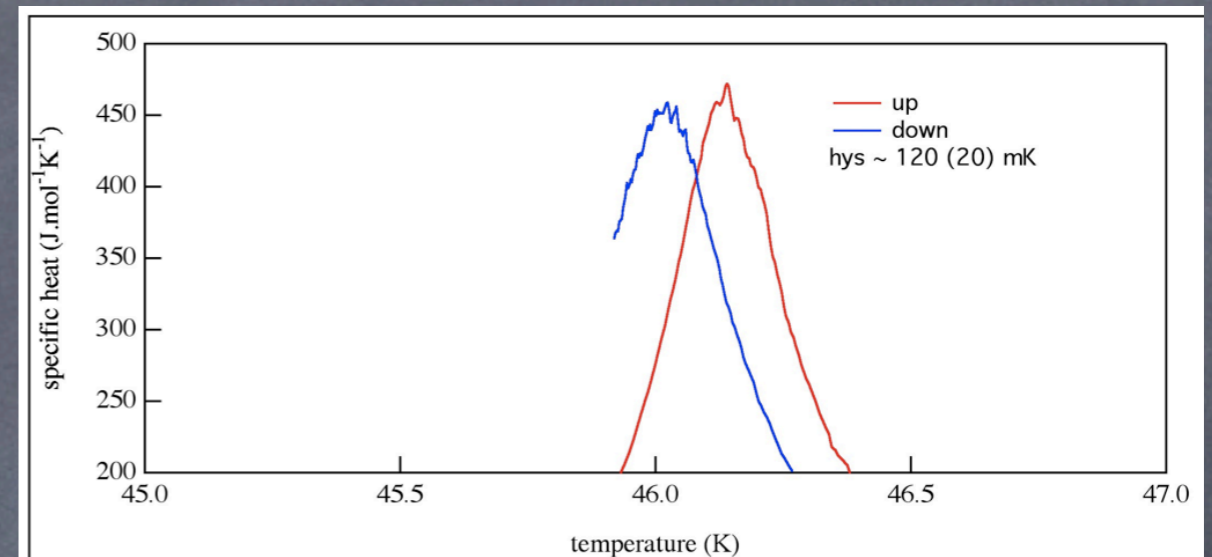
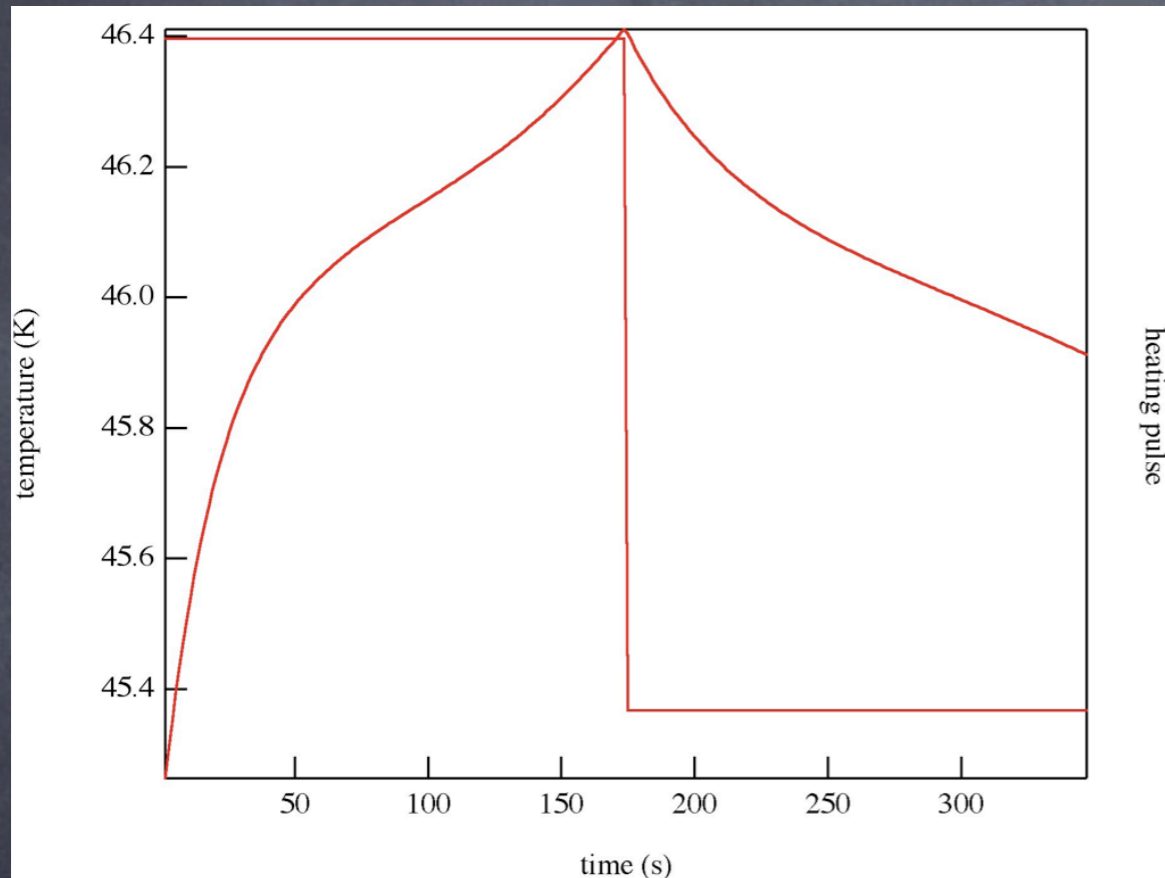
# (Dis) Advantages,

- popular, reliable, and widely used at low T
- extended down to below 10mK (J.P. Brison)
- good accuracy (5%), but not excellent resolution
- mass down to a fraction of a mg
- relaxation time  $\geq 1s$
- $C_p$  can vary by orders of magnitude between the interesting T-range, so does relaxation time
- Point by point, long and tenuous, 1pt at 100K=20mins



# AuCrS<sub>2</sub> : antiferromagnetic + structural

Courtesy:  
F. levy  
CNRS-grenoble





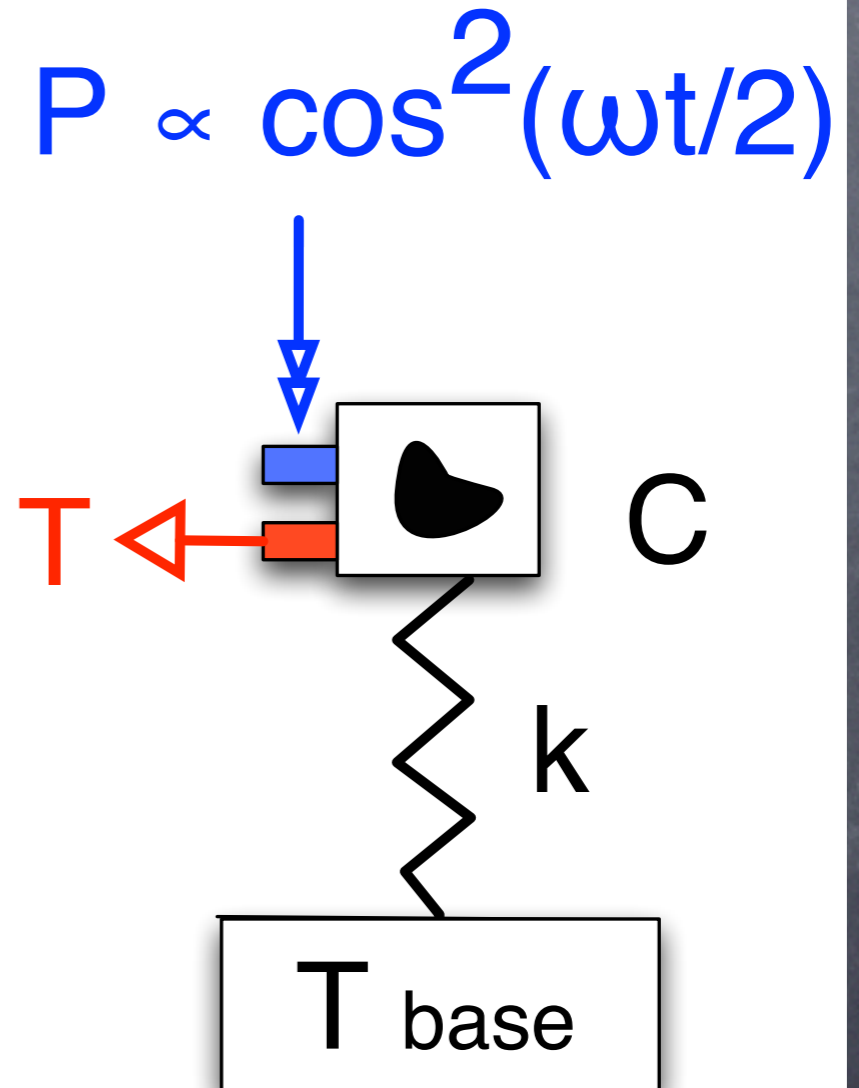
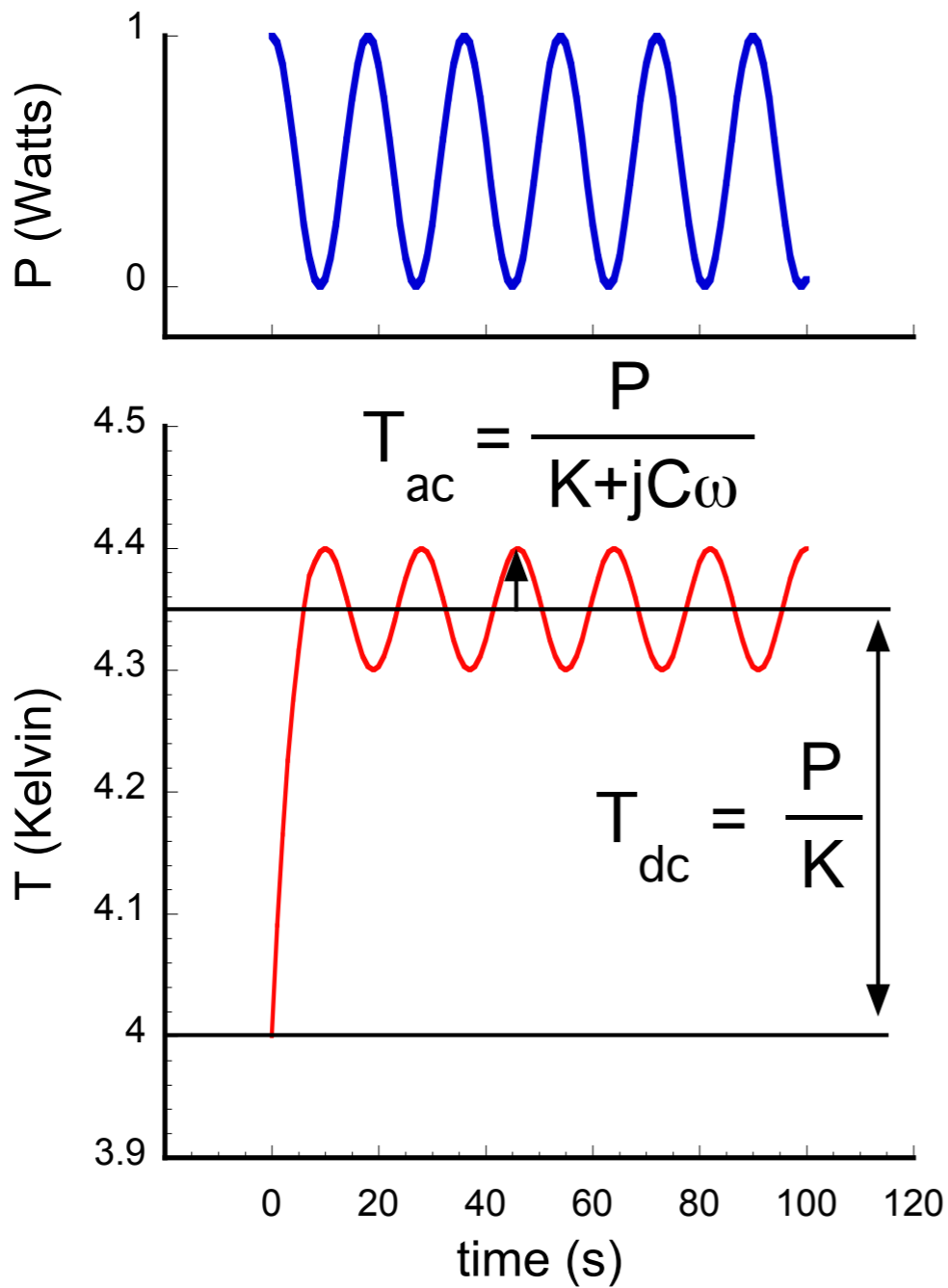
# Options

- define internal and external time constants
- choose duration time vs  $\tau_{int}$  and  $\tau_{ext}$
- fitting procedure : introduce constrains
- Large relaxations and local  $dT/dt$  (A. Demuer)  
faster, larger current,...
- Dual Slope method (dynamic, no calibration of  $\kappa$ )



# Modulation (alternative)

## ac-power



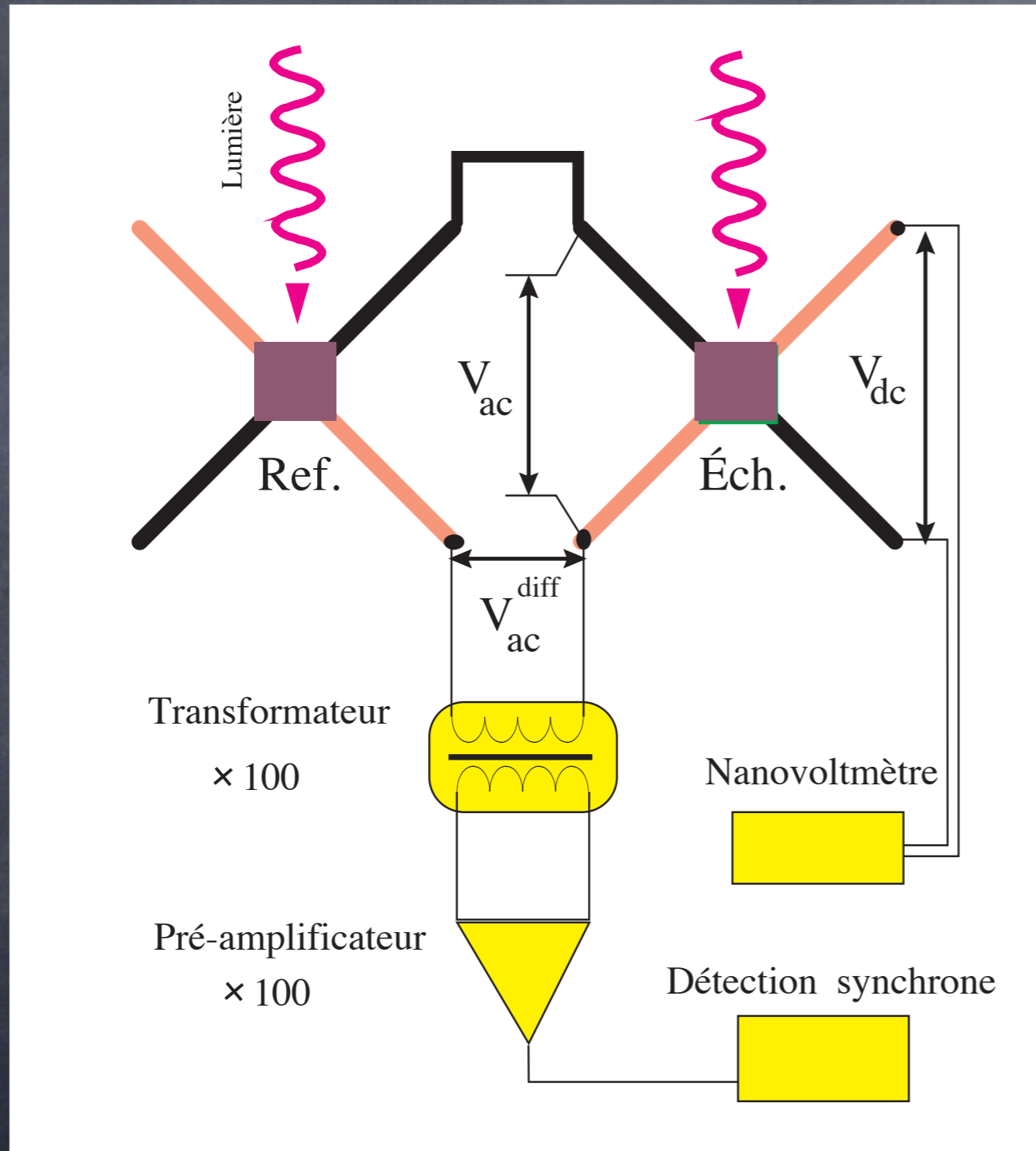


# Characteristics

- lock-in detection, filters, noise rejection (true for all modulation techniques)
- excellent resolution (typical  $10^{-4}$ ), lesser accuracy but  $\Delta C = \text{a few } 10^{-12} \text{ J/K}$
- 100 nanogram  $< m <$  a few milligram
- continuous: during H and/or T sweeps
- easy to extend a differential configuration
- extrem conditions: 45T-DC, pulsed 60T, 15Gpa, 10kHz



# Schematic



- transformer at room T:  
a few  $0.1 \text{ mK}/(\text{Hz})^{1/2}$
- transformer at 4K:  
a few  $10 \text{ } \mu\text{K}/(\text{Hz})^{1/2}$
- Squid detection:  
a few  $0.1 \text{ } \mu\text{K}/(\text{Hz})^{1/2}$